

# Image Compression

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[1]: #Nilava Metya
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      #Python 3
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```
[2]: import numpy as np
      from PIL import Image as im
      import matplotlib.pyplot as plt
```

```
[3]: image = im.open('conway.jpg')
      A = np.array(image, dtype=float) / 255.0
      A = np.dot(A, [0.2989, 0.5870, 0.1140])
      m,n = A.shape
```

```
[4]: U, S, Vt = np.linalg.svd(A)           #do the SVD
      K = [40,80,120,160]                 #storing values of k
      l = len(K)
      S = np.diag(S)                       #original S is only a linear
      ↪array, need to convert to matrix
```

```
[5]: approx = []
      for i in range(l):
          approx.append(U[:, :K[i]] @ S[:K[i], :K[i]] @ Vt[:K[i], :])
      ↪#taking approximations
```

```
[6]: #obtaining and printing a table for Frobenius norm of differences
      error = [0 for _ in range(l)]
      print("k\t|\t Frobenius norm")
      print("-----+-----")
      for i in range(len(K)):
          error[i] = np.linalg.norm(A-approx[i])
          print(str(K[i])+"\t|\t"+str(error[i]))
```

k		Frobenius norm
40		31.733288485394482
80		19.016427727768185
120		13.055854194249326
160		9.511015173570117

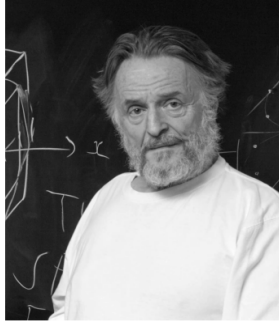
```
[7]: fig, ax = plt.subplots(len(K)+1, 1, figsize = (10, 30))

ax[0].set_title("Original Picture")
ax[0].imshow(A, cmap = 'gray')
ax[0].axis('off')

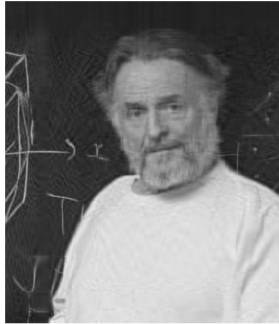
for i in range(1):
    ax[i+1].imshow(approx[i], cmap = 'gray')
    ax[i+1].set_title("k = " + str(K[i]))
    ax[i+1].axis('off')

plt.show()
```

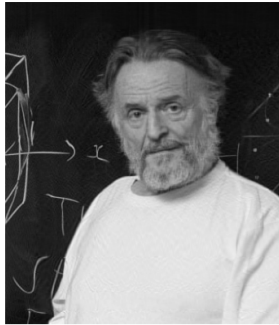
Original Picture



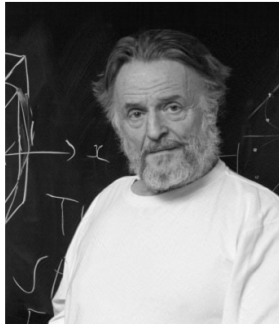
$k = 40$



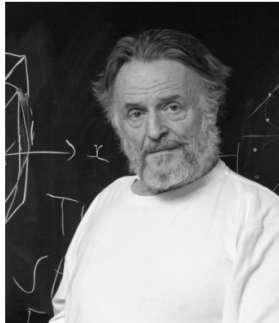
$k = 80$



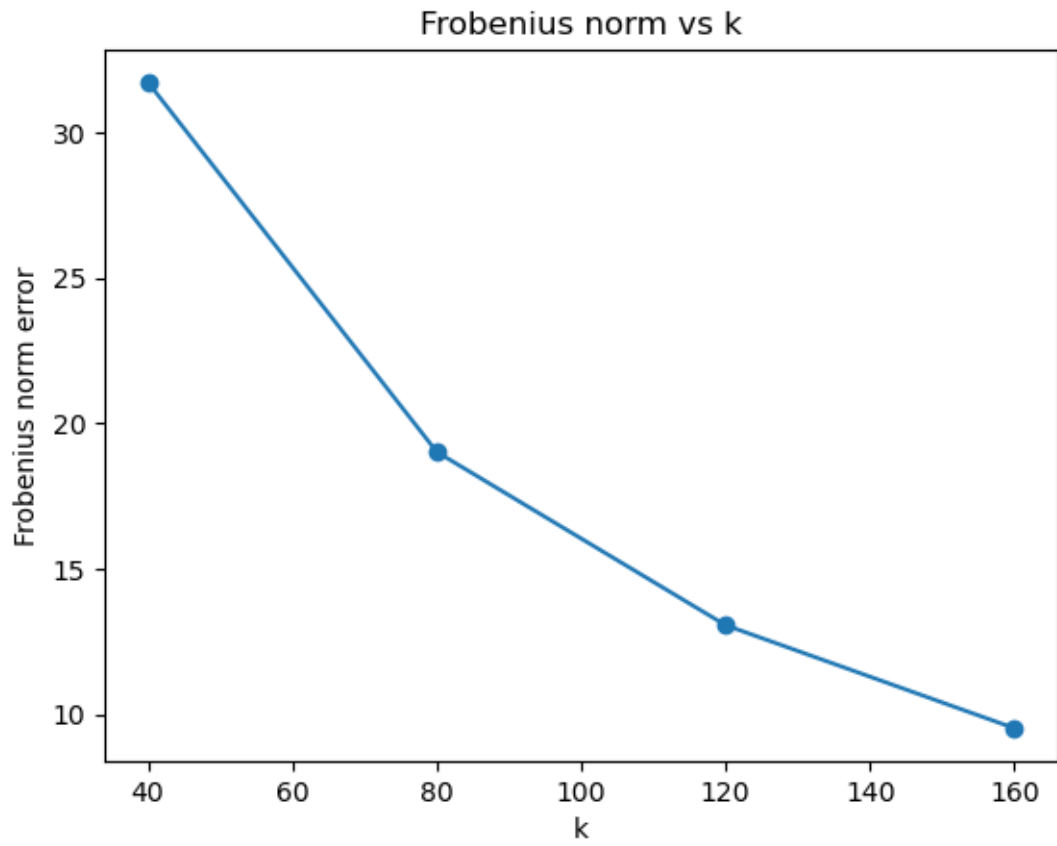
$k = 120$



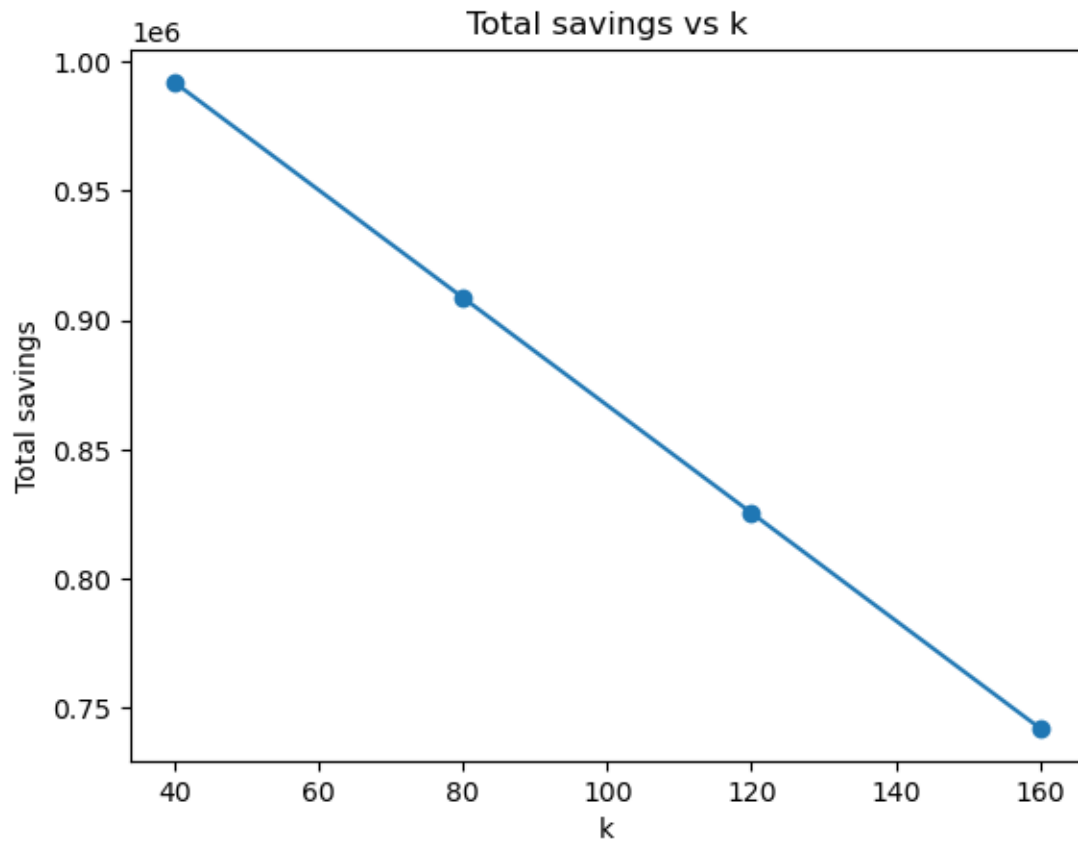
$k = 160$



```
[8]: plt.plot(K, error, marker = 'o')
plt.xlabel('k')
plt.ylabel('Frobenius norm error')
plt.title("Frobenius norm vs k")
plt.show()
```



```
[9]: plt.plot(K, [m*n-(m+n+1)*k for k in K], marker = 'o')
plt.xlabel('k')
plt.ylabel('Total savings')
plt.title("Total savings vs k")
plt.show()
```



```
[10]: plt.imshow('A160.jpg', approx[3], cmap = 'gray')
plt.imshow('original.jpg', A, cmap = 'gray')
```